Loss features in ultracold ¹⁶²Dy gases: Two- versus three-body processes

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Dipolar gases like erbium and dysprosium have a dense spectrum of resonant loss features associated with their strong anisotropic interaction potential. These resonances display various behaviors with density and temperature, implying diverse microscopic properties. Here we quantitatively investigate the low-field ($B < 6\,\mathrm{G}$) loss features in ultracold thermal samples of $^{162}\mathrm{Dy}$. The atoms are spin polarized in their lowest internal state so that pure two-body losses due to spin relaxation are forbidden. However, our analysis reveals that some resonances lead to a two-body-like decay law, while others show the expected three-body decay. We present microscopic one-step and two-step models for these losses, investigate their temperature dependence, and detect a feature compatible with a d-wave Fano-Feshbach resonance that has not been observed before. We also report the variation of the scattering length around these resonances, inferred from the time-of-flight expansion of the condensate.

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I. INTRODUCTION

Quantum gases are by definition relatively short lived, as these systems are extremely sensitive to loss processes such as collisions with residual gases, photoassociation, or inelastic collisions. Three-body losses, for example, correspond to inelastic recombination in which three particles interact sufficiently strongly to form a two-body bound state (dimer), while the third particle ensures energy conservation by acquiring a kinetic energy equal to the potential energy difference. This energy is usually much greater than the trap depth, resulting in the effective loss of all three particles. Such a mechanism is enhanced close to a scattering resonance. In inhomogeneous gases, three-body losses are particularly damaging, as they lead to the depletion of the denser part of the atomic cloud, resulting in antievaporative cooling [1,2]. However, while this process limits the timescales over which ultracold dense systems can be studied, it also provides an insight into the few-body physics of strongly interacting cold gases, which remains a challenging and stimulating area of research [3–8].

Dipolar gases like chromium, dysprosium, erbium, and thulium possess a large dipolar magnetic moment, resulting in properties that markedly differ from those of alkali atoms. In these systems, long-range anisotropic dipolar interactions lead to new features of the collision potential, such as the emergence of a $1/R^4$ potential [9] or the modification of the van der Waals C_6 coefficient [10]. This anisotropic dipolar interaction can lead to striking new behaviors, such as low-temperature d-wave Fano-Feshbach resonances [11]. Furthermore, the anisotropic interaction potential is responsible for the dense spectrum of loss resonances 1 in ultracold gases of erbium,

In this article we investigate the few-body processes driving the large number of low-field loss features in ultracold gases of ¹⁶²Dy. We recover the 9 previously reported resonances for this isotope [12] as well as 10 extra features, and quantitatively characterize the dependence on atom number and temperature for 11 features, indicated by the red vertical lines in Fig. 1. In addition, we identify a loss feature compatible with a *d*-wave Fano-Feshbach resonance, with similar characteristics to those reported for chromium in Ref. [11]. We also measure the three-body loss rate parameter for a Bose-Einstein condensate (BEC) near zero magnetic field. This low-field zone is especially interesting if the objective is to establish spin-orbit coupling in a dysprosium gas, similar to [20], while preventing two-body spin relaxation at increased atomic densities. Finally, we complement our analysis with a study of the BEC expansion near the different loss features, interpreting the dilatation of the cloud as a signature of enhanced two-body interactions.

II. LOW-FIELD LOSS FEATURES

Experimentally, we load about 4×10^6 dysprosium atoms (162 Dy) into a crossed dipole trap formed by laser beams operating at a wavelength $\lambda=1064$ nm. The atoms are loaded from a five-beam compressed magneto-optical trap (MOT)

dysprosium, and thulium [12–16]. A precise characterization of loss features has recently regained interest, triggered by the determination of the temperature dependence of their chaotic statistics [15,17], the optimization of the evaporative cooling [18], and the identification of appropriate Fano-Feshbach resonances in dipolar mixtures [19].

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¹Here we refer to these resonances as loss features instead of Fano-Feshbach resonances to allow for the possibility that some loss

features are not associated with a change in the two-body scattering length but are instead a genuine three-body effect.

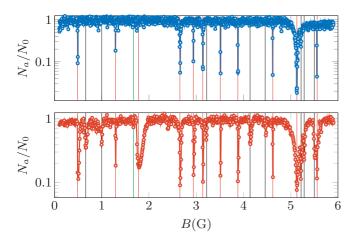


FIG. 1. Normalized atom number as a function of magnetic field for a thermal sample with temperature $T=190\,\mathrm{nK}$ (top panel in blue) and $T=2.4\,\mu\mathrm{K}$ (bottom panel in red). The red vertical lines indicate the 11 loss features for which we characterize the density and temperature dependence.

with atom number $N_a \approx 1 \times 10^8$ and temperature $T \approx 15 \,\mu\text{K}$ (see Appendix B for more details).

After forced evaporative cooling, we produce an ultracold thermal gas, spin polarized in the Zeeman sublevel of lowest energy $|J, m_J = -J\rangle$, with atom number $N_a = 2 \times 10^5$ and temperature $T \sim 190 \, \text{nK}$, above the condensation threshold. The evaporation is carried out with a fixed magnetic field of 1.660 G, indicated by the green vertical line in Fig. 1. We then quench the magnetic field to a target value and hold the cloud for 2 s. We measure the atom number and temperature after time-of-flight absorption imaging, which gives us information about both the losses and heating of the cloud. The magnetic field is scanned from 0 to 6 G, and we measure the atom number variation as a function of the magnetic field B. For this low temperature, we identify ten loss features, corresponding to the atom number drops in Fig. 1, top panel. These resonances, except for one, have been reported in Ref. [12].

A similar experiment is performed for a hotter thermal cloud with temperature $T = 2.4 \,\mu\text{K}$. We recover the previous resonances and observe several new loss features (lower panel in Fig. 1), increasing the total number of loss features count to 19. This result qualitatively demonstrates the nontrivial emergence of temperature-dependent loss features in an ultracold gas of dysprosium [12].

To probe different temperatures T, we use a protocol that differs from most previous investigations of resonant losses in lanthanides by preparing all of our samples in the same optical potential regardless of T. We do this by (i) cooling the atoms to very low temperature (\sim 200 nK), (ii) adiabatically recompressing the optical trap to a large depth, and (iii) tuning the temperature by parametric heating of the trapped gas. Before measuring the remaining atom number, we ensure that the cloud is in thermal equilibrium by holding it for 0.5 s, which is long compared to the elastic collision time. By contrast, many previous studies adjusted temperature by halting the evaporation process at varying laser intensities. Our protocol addresses a potential bias resulting from differences in polarizability between free atoms and the bound state

involved in the loss process [17]. Additionally, it is advantageous to operate at a high trap depth U_0 , leading to a large ratio $\eta = U_0/k_{\rm B}T$. This effectively reduces the losses due to evaporation that could potentially obscure distinctive features resulting from the loss resonances we seek to examine.

III. MICROSCOPIC DESCRIPTION OF LOSS FEATURES

Before continuing with our experimental analysis, let us summarize the models developed in Refs. [5,11,14,21] that have been used to characterize loss features in dipolar gases. First we recall that for our polarized, low-temperature sample, a pure two-body decay process

$$A + A \rightarrow A_2^{\text{bound}},$$
 (1)

where $A_2^{\rm bound}$ is a bound dimer (negative energy), is impossible because of energy-momentum conservation. The models of Refs. [5,11,14,21] assume as an intermediate step the resonant formation of a dimer or a trimer, and they lead to different scaling laws of the maximal loss rate with density, as we show now. To keep the analysis simple, we assume here a uniform atomic density n_a , but the following results can then be readily transposed to the case of a harmonically trapped gas.

A. The resonant dimer model

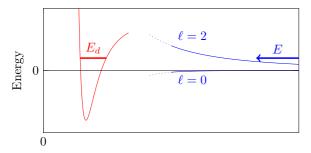
We describe a sequential process involving two steps: (i) a quasi-resonant coupling between a state with two free atoms and a state where a dimer in some excited state A_2^* is formed,

$$A + A \rightleftharpoons A_2^*,$$
 (2)

and (ii) the decay of the dimer with a rate Γ_d . This decay is essentially induced by the collision with a third atom, $A_2^* + A \rightarrow A_2 + A$, so that Γ_d is implicitly a function of n_a , and where A_2 is a deeply bound dimer.

In the following we restrict ourselves to the case of large Γ_d so that the dimer A_2^* decays soon after its formation by the direct process in (2), and the reverse process in (2) does not play a significant role. This scenario can happen in the case of a narrow Fano-Feshbach resonance and a sufficiently large atomic density n_a . We will see that it is the relevant one for most of the resonances observed in our experimental conditions, and we refer the reader to Refs. [5,11,21,23] for a discussion of the general case and in the limit of small Γ_d (see also Appendix A). Note that the situation considered here is the opposite of that of Ref. [24], where the atoms A formed a Bose-Einstein condensate and where the authors could observe a coherent oscillation between the two members of Eq. (2), thanks to bosonic stimulation.

To model the process (2), we consider a fictitious box containing two atoms, whose typical volume is thus $L^3 = 2/n_a$, where n_a is the atomic density. We work in the center-of-mass frame of the two atoms, and we denote E the energy of the relative motion of the colliding atoms. We suppose that the resonant process (2) occurs for an incident partial wave ℓ , and we introduce the coupling matrix element $\hbar \kappa$ between the relative wave function of the two free atoms and the wave function of the dimer state, of energy E_d (see Fig. 2). Each wave function is supposed to be normalized to unity in the box L^3 . We will not try to provide here a detailed expression



Interparticle distance r

FIG. 2. Resonant dimer model. A pair of atoms, with relative motion of energy E and angular momentum ℓ , can resonantly form a dimer state of energy $E_d \approx E$, which then decays at a rate Γ_d . In the case of a narrow Fano-Feshbach resonance [22], this process leads to a sharp energy feature described by the Lorentzian of Eq. (6).

for κ , and we simply note its scaling with energy and box size: $\kappa \propto (E^\ell/L^3)^{1/2}$ [25]. The Hamiltonian of this fictitious two-level system is thus the 2×2 matrix

$$\begin{pmatrix} E & \hbar \kappa \\ \hbar \kappa^* & E_d - i\hbar \Gamma_d/2 \end{pmatrix}, \tag{3}$$

where we have added the imaginary term $-i\hbar\Gamma_d/2$ to the dimer energy to account for its instability (see also Appendix A for an approach of the same problem with rate equations). The two eigenvalues of this matrix are complex, which expresses the fact that the scattering state A + A is now also unstable because of its coupling to A_2^* .

The imaginary part of the energy of the A+A pair in the presence of the coupling κ gives the decay rate of this pair, which reads for $\Gamma_d \gg \kappa$ (Breit-Wigner formula),

$$\Gamma_a \approx \frac{\Gamma_d |\kappa|^2}{(E - E_d)^2 / \hbar^2 + \Gamma_d^2 / 4},\tag{4}$$

from which we deduce the scaling of the total loss rate in the sample with N_a atoms at a given energy E,

$$\dot{N}_a \propto -N_a \Gamma_a \propto -n_a N_a E^{\ell} \mathcal{L}(E - E_d),$$
 (5)

where \mathcal{L} stands for the Lorentzian function,

$$\mathcal{L}(x) = \frac{1}{2\pi} \frac{\hbar \Gamma_d}{x^2 + (\hbar \Gamma_d/2)^2}.$$
 (6)

We now average the rate (5) over a thermal distribution of temperature T so that the loss rate \dot{N}_a is proportional to

$$\frac{\int_{0}^{+\infty} dE \ \rho(E) \ E^{\ell} \ \mathcal{L}(E - E_{d}) \ e^{-E/k_{\rm B}T}}{\int_{0}^{+\infty} dE \ \rho(E) \ e^{-E/k_{\rm B}T}},\tag{7}$$

with the density of states $\rho(E) \propto \sqrt{E}$ for the relative motion of the A+A pair. The expression (7) is in general a complicated function of E_d and Γ_d (and thus n_a). An interesting limiting case is obtained when the resonance width $\hbar\Gamma_d$ is very small compared to k_BT , in which case the Lorentzian function $\mathcal{L}(E-E_d)$ can be replaced by a Dirac function $\delta(E-E_d)$ in (7). In this case, we find that the decay rate resembles a two-body loss process [11],

$$\dot{N}_a = -L_2 n_a N_a,\tag{8}$$

with an effective two-body loss parameter L_2 given by

$$L_2(E_d, T) \propto T^{-3/2} E_d^{\ell+1/2} e^{-E_d/k_B T}$$
. (9)

The experimental procedure involves scanning the value of E_d by ramping the magnetic field at a given temperature and searching for the maximal loss rate. From the scaling of Eq. (9), we find that the maximum loss rate occurs for $E_d = (\ell + 1/2)k_BT$ with

$$L_2^{(\text{max})}(T) \propto (k_B T)^{\ell-1}.$$
 (10)

Assuming the two hypotheses above are valid, i.e., $\hbar\kappa \ll \hbar\Gamma_d \ll k_BT$, the variation of $L_2^{(\text{max})}$ with temperature thus gives immediate access to the partial wave ℓ involved in the resonant loss process. The validity of these hypotheses can be checked by verifying that \dot{N}_a/N_a scales linearly with n_a [see Eq. (8)].

B. The resonant trimer model

The second model consists of a pure three-body process [14]. Three particles that do not have resonant pairwise interactions arrive through a three-body open channel \mathcal{O}_1 , with the quantum number λ associated with the grand angular momentum, and an incoming energy E close to the energy E_t of an excited trimer state A_3^* , residing in a closed channel C:

$$A + A + A \rightleftharpoons A_3^*. \tag{11}$$

If we neglect atom interactions at long distance, the incoming channel is purely repulsive, even for $\lambda=0$, with the three-body centrifugal potential $V(R) \propto [\lambda(\lambda+4)+\frac{15}{4}]/R^2$, where R is the hypergeometric radius [26,27]. The closed channel \mathcal{C} is coupled to other channels \mathcal{O}_f that are not directly coupled to the incoming open channel, thereby determining the decay rate Γ_t of the trimer A_3^* . Note that since we do not assume resonant two-body interactions, the trimer A_3^* differs from Efimov trimers. The latter play an important role in broad Fano-Feshbach resonances and lead to the $1/T^2$ dependence of the three-body loss rate L_3 [1,28].

The analysis of this process follows along the same general lines as for the resonant dimer model. We consider a fictitious box of volume $L^3 \sim 3/n_a$ containing three particles. The coupling κ between the incoming state of energy E and the resonant trimer state now scales as $\kappa \propto E^{\lambda/2}/L^3$, and the width Γ_t of the trimer state A_3^* induces a nonzero width for the incoming state A+A+A, given by a formula similar to (4). We are then led to $\dot{N}_a = -n_a^2 N_a E^\lambda \mathcal{L}(E-E_t)$, where \mathcal{L} is the Lorentzian function similar to (6) with width Γ_t [14,29,30]. The thermal average of this decay rate involves the three-particle density of state $\rho(E) \propto E^2$ so that we obtain, in the limit $\hbar \Gamma_t \ll k_B T$,

$$\dot{N}_a = -L_3 n_a^2 N_a,\tag{12}$$

with the scaling $L_3 \propto T^{-3} E_t^{\lambda+2} e^{-E_t/k_B T}$. When scanning the energy of E_t by ramping the external magnetic field, the max-

²Note, however, that the scaling in E^{λ} has been questioned for nonzero values of λ by [30] for some specific cases.

imum loss rate scales as

$$L_3^{\text{max}}(T) \propto (k_{\text{B}}T)^{\lambda - 1},\tag{13}$$

and it is obtained for $E_t = (\lambda + 2) k_B T$.

Discussion. Although the scaling of the loss rate with temperature is similar in both models of Secs. III A and III B, the latter is a pure three-body process and therefore cannot predict two-body dominated features of the type $\dot{N}_a/N_a \propto -n_a$. The reverse statement may not be true: References [5,11,23] indicate that the resonant dimer model can lead to an effective three-body loss rate $\dot{N}_a/N_a \propto -n_a^2$ in the case where the excited bound state is long-lived relative to its coupling to the incoming open channel. Let us also emphasize that the simple scaling laws (10,13) hold only when $\hbar\kappa \ll \hbar\Gamma_{d,t} \ll k_BT$. If this is not the case, the variation of $L_{2,3}^{(max)}$ with temperature is nontrivial.

IV. LOSSES VS DENSITY AND TEMPERATURE

In this section we present our experimental results regarding the loss rates in a harmonically trapped ¹⁶²Dy gas due to inelastic processes. We first outline our methodology (Sec. IV A), then investigate the variations of the loss rate with density at a given temperature (Sec. IV B), and then with temperature at a given atom number (Sec. IV C). We summarize our results for the whole set of resonances in Sec. IV D.

A. Methodology

We recall that the microscopic nature of the process (two or three-body loss) of each resonance is unknown, as is the temperature variation of the associated loss rate $[L_2(T)$ or $L_3(T)]$. Therefore, for a gas prepared with a given atom number N_a and temperature T, we restrict our analysis of the decay rate to a short time interval Δt , during which N_a and T vary by less than 20% and 30%, respectively. A linear fit $N_a(t) = N_0(1-\beta t)$ to the decaying atom number over this interval then allows us to derive the decay rate $\dot{N}_a \approx \Delta N_a/\Delta t$ for a density \bar{n}_a and a temperature \bar{T} taken equal to the average value of these quantities over the time interval Δt . The interval retained for the fit is indicated by a colored zone in Figs. 3 and 4.

In addition, we recall that the volume of a trapped gas in a harmonic potential is a function of the temperature. If interactions play a negligible role, one finds $V = (2\sqrt{3}\pi k_{\rm B}T/m\bar{\omega}^2)^{3/2}$, where $\bar{\omega} = (\omega_x\omega_y\omega_z)^{1/3}$ is the geometric mean of the trapping frequencies and $k_{\rm B}$ the Boltzmann constant. In the following, we designate by $n_a = N_a/V$ the average density in the trap. For a fixed temperature, the volume does not vary, and $\beta = -\dot{N}_a/N_a$ scales as $\beta \propto n_a^{\gamma}$ with $\gamma = 1$ (resp. $\gamma = 2$) in the case of a two-body (resp. three-body) dominated loss process (8) [resp. (12)].

B. Examples at fixed T: Two-versus three-body dominated losses

Here we describe a typical analysis procedure of one of the resonances featured in Fig. 1, specifically, the

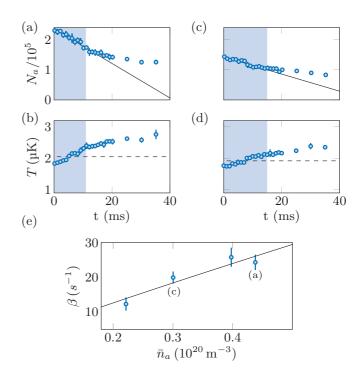


FIG. 3. Atom loss dynamics for varying total atom number N_a at a magnetic field $B=5.130\,\mathrm{G}$. The averaged temperature is constant and equal to $T\approx 2.0(1)\,\mu\mathrm{K}$. Panels (a) and (b) show the atom number and temperature evolution for the case of an initial atom number $N_0=2.3\times10^5$. Panels (c) and (d) show the atom number and temperature evolution for $N_0=1.4\times10^5$. (e) Variation of the initial loss rate, $\beta=-\dot{N}_a/N_a$, with the density $\bar{n}_a\propto\bar{N}_a/\bar{T}^{3/2}$. The solid line is the fitting function $\beta\propto\bar{n}_a^{\gamma}$ with $\gamma=0.92(10)$.

resonance occurring at a magnetic field strength of $5.130\,\mathrm{G}$. As explained in Sec. II, we prepare a sample with an adjustable atom number at the desired temperature. The depth of the trap is sufficient to render losses due to evaporation insignificant.³ We jump the magnetic field from its initial value ($B = 1.660\,\mathrm{G}$) to a magnetic field close to the target loss feature (typically $100-200\,\mathrm{mG}$ away from it). We then wait for $500\,\mathrm{ms}$ and perform a second quench towards the magnetic field for which the losses are maximum. This sequence allows a better resolution of the initial loss dynamics.

We show in Figs. 3(a) and 3(c) two decay curves $N_a(t)$ for two initial atom numbers, hence two atomic densities n_a . Figures 3(b) and 3(d) show the corresponding changes in temperature. A linear fit of the short-time variation of N_a provides the decay rate β introduced in Sec. IV A. We summarize our results for β as a function of n_a in Fig. 3(e). A fit $\beta(n_a) = \beta_1 n_a^{\gamma}$ gives $\gamma = 0.92(10)$, an indication of a two-body dominated loss feature for this particular resonance.

To cross-validate our methodology, we have performed a similar loss measurement for a thermal gas at $B = 1.660 \,\mathrm{G}$, i.e., away from any loss resonance. We measure $\gamma = 2.3(4)$, which is consistent with a three-body loss process, as expected

 $^{^3}We$ have independently estimated the lifetime of our vacuum system to be $\tau\gtrsim15\,\text{s}.$

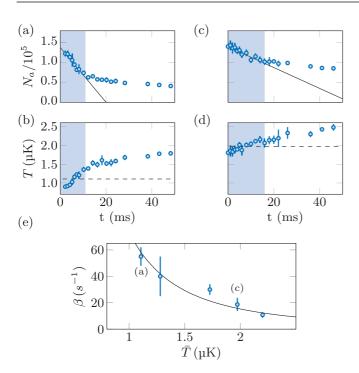


FIG. 4. Atom losses as a function of temperature T for a fixed atom number $N_a \approx 1.5 \times 10^5$, for the loss feature $B = 5.130\,\mathrm{G}$. (a) and (b) Atom number and temperature evolution, respectively, for a thermal cloud with temperature $\bar{T} = 1.1(1)\,\mu\mathrm{K}$. (c) and (d) Atom number and temperature evolution for $\bar{T} = 2.0(1)\,\mu\mathrm{K}$. (e) Variation of the initial loss rate, $\beta = -\dot{N}/N$, with temperature. The solid line is the fitting function $\beta \propto T^a$, with $\alpha = -2.2(3)$.

for a gas with positive background scattering length. We find, for a thermal gas, $L_3 = 1.2(2) \times 10^{-40} \text{ m}^6/\text{s}$.

The same technique allows us to determine the three-body loss coefficient of a BEC either close to B=0 or at $B=1.660\,\mathrm{G}$ away from any loss resonance. For that purpose we evaporate until we produce a quasi-pure BEC and then adiabatically recompress the trap to a final trap depth of $2.16\,\mu\mathrm{K}$, with frequencies equal to $\{\omega_x,\,\omega_y,\,\omega_z\}=2\pi\times\{49,\,152,\,115\}\,\mathrm{Hz}$. We find $L_3=2.9(3)\times10^{-41}\,\mathrm{m}^3/\mathrm{s}$ and $L_3=5.0(8)\times10^{-41}\,\mathrm{m}^3/\mathrm{s}$ for the background three-body loss rate, $B=1.660\,\mathrm{G}$, and the near-zero field $B\lesssim50\,\mathrm{mG}$, respectively. The values of L_3 are extracted for a BEC fraction going from near unity to 0.5. Compared to a thermal sample, we find a reduction of L_3 in qualitative agreement with the predicted 3! reduction for a pure BEC [31].

C. Example at fixed N_a : T-dependent loss rate

We now turn to the temperature dependence of the atom loss rate, still taking the resonance at $B = 5.130 \,\text{G}$ as an example. Following the procedure outlined in Secs. II and IVB, we prepare thermal samples at different temperatures but with the same atom number. We plot in Fig. 4(a) [resp. Fig. 4(c)] the atom number decay for the initial temperature $T = 0.9 \,\mu\text{K}$ [resp. $T = 1.8 \,\mu\text{K}$]. We show in Figs. 4(b) and 4(d) the corresponding time evolution of the temperature.

As explained in Sec. IV A, we restrict our analysis to the short time evolution and extract the rate $\beta = -\dot{N}_a/N_a$ from a linear fit to the measured decay of $N_a(t)$. The values of β

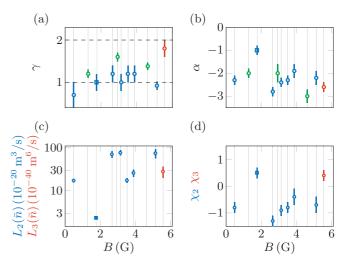


FIG. 5. Summary of density and temperature dependence for 11 loss features between 0 and 6 G. (a) Determination of two- vs three-body dominated loss features. A value of γ compatible with 1 indicates a two-body dominated loss feature, while a value of $\gamma = 2$ indicates a three-body dominated feature. These values are represented by dashed horizontal lines. Loss features characterized by s(d)-wave two-body dominated loss processes correspond to blue circles (squares), while red circles correspond to three-body processes. The green circles indicate loss features in a transitional regime where it is not possible to determine a two- or three-body loss rate. (b) Temperature dependence of the loss rate $\beta(T) \propto T^{\alpha}$. (c) Strength of the different loss features. From the results shown in (a) and (b) we derive the two-body and three-body loss rates for a nominal density of $\bar{n} = 1 \times 10^{20} \,\mathrm{m}^{-3}$ and temperature $\bar{T} = 1 \,\mathrm{\mu K}$. (d) Temperature dependence of the two- and three-body loss coefficients $\chi_2 = \alpha + 3/2$ (blue) and $\chi_3 = \alpha + 3$ (red). The 11 loss features studied in this article are marked by vertical bars.

for different temperatures are shown in Fig. 4(e). We fit the relation $\beta(T) = \beta_2 T^{\alpha}$ to the temperature dependence of the loss rate, with $\alpha = -2.2(3)$. From the analysis of Sec. IV B, we know that this particular resonance is likely to be due to a two-body loss decay $\dot{N}_a = -L_2 n_a N_a$, and hence $\beta \propto L_2/V$ for a given N_a . Recalling that the volume in a harmonic trap scales as $V \propto T^{3/2}$, we infer that $L_2(T) \propto T^{\chi_2}$ with $\chi_2 = \alpha + 3/2 \approx -0.7(3)$ for this particular resonance.

D. Analysis of all loss resonances

The same procedure regarding the dependence with density and temperature is applied to the ten loss features observed in Fig. 1 (top panel) plus the loss feature at 1.755 G, which emerges for hotter clouds (see Fig. 1, bottom panel). These 11 loss features are identified by the red vertical lines in Fig. 1. We report in Fig. 5(a) the exponent γ for each loss feature (with $\beta = -\dot{N}_a/N_a \propto n_a^{\gamma}$ at a fixed averaged temperature \bar{T}) and in Fig. 5(b) the exponent α (with $\beta \propto T^{\alpha}$ at a fixed initial N_a).

From the results shown in Fig. 5(a), we identify seven loss features for which the measured value of γ is compatible, within error bars, with a two-body dominated process, i.e., $\gamma = 1$. We identify a single loss feature for which γ is compatible, within error bars, with a three-body dominated

process, i.e., $\gamma=2$. We also identify three loss features that are not clearly described by either two- or three-body processes. This behavior can emerge, for example, in the case of the two-step process discussed in Sec. III A when the decay rate of the dimer Γ_d is comparable to the rate of the process (2) producing this dimer. We will not attempt to describe the temperature dependence of those three lines.

Once the assignment of a two-body or three-body resonance has been made from the variation of β with n_a , we determine the temperature dependence of the associated two-or three-body loss rates, $L_2 \propto \beta V$ or $L_3 \propto \beta V^2$, for a given N_a . Since the volume scales as $T^{3/2}$, we write the temperature dependence of the two- and three-body loss rates as $L_2 \propto T^{\chi_2}$ and $L_3 \propto T^{\chi_3}$, where $\chi_2 = \alpha + 3/2$ and $\chi_3 = \alpha + 3$.

In Fig. 5(d) we observe that six out of the seven identified two-body processes have a rate L_2 compatible with a 1/T dependence, as expected for s-wave resonances [see Eq. (10) for $\ell = 0$]. These resonances are marked with blue circles in the various panels of Fig. 5.

The only exception is the previously unobserved Fano-Feshbach resonance at $B=1.755\,\mathrm{G}$, marked as a blue square in the various panels of Fig. 5. Its rate scales as $L_2 \propto T^{0.5}$. Although the scaling with temperature is strictly speaking not compatible with a d-wave resonance for which we would expect $L_2 \propto T$, as observed for chromium [11], we suggest that the deviation of $\chi_2 \approx 0.5\,\mathrm{from}\,1$ is due to the weakness of the loss feature. As shown in Fig. 5(c), this resonance is an order of magnitude weaker than the other resonances, and therefore our measurements may be contaminated by other loss processes, such as forced evaporation, which could tend to weaken the observed temperature dependence.

For the six two-body loss features compatible with an s-wave resonance (blue circles in Fig. 5), one might expect a shift of the center of the resonance with temperature, given by $\Delta B = k_{\rm B} \Delta T/\delta \mu$, where $\delta \mu$, the differential magnetic moment between open and closed channels, is a priori unknown. Given the recent determination of $\delta \mu \approx 1000 \, \mu {\rm K/G}$ for the case of thulium [17], we would expect a magnetic field shift \sim mG for our temperature range. This shift is comparable to our magnetic field stability and thus is difficult to detect on our platform.⁴

Finally, for the three-body dominated loss feature, identified in red in Fig. 5, we report a small positive temperature dependence. At this stage we cannot conclude whether this feature is caused by a direct three-body resonance, as described in Sec. III B, or whether it corresponds to an effective three-body decay resulting from a particular parameter setting in a two-step two-body loss process as proposed in [5,11,21,23].

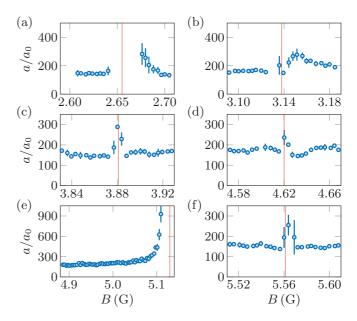


FIG. 6. Variation of the scattering length with magnetic field, in the vicinity of six loss features. Central magnetic field: (a) $B = 2.655 \,\text{G}$, (b) $B = 3.138 \,\text{G}$, (c) $B = 3.881 \,\text{G}$, (d) $B = 4.620 \,\text{G}$, (e) $B = 5.130 \,\text{G}$, and (f) $B = 5.561 \,\text{G}$.

V. BEC EXPANSION NEAR A LOSS FEATURE

Finally, we report a complementary measurement that allows us to determine the *s*-wave scattering length if we suppose that the interactions are of a two-body nature, as it seems to be the case for at least 7 out of 11 resonances. We perform a long time-of-flight expansion of a BEC of ¹⁶²Dy and infer the scattering length from its area in the x-y plane orthogonal to the bias magnetic field pointing along z. The BEC is created in a trap with angular frequencies $\{\omega_x, \omega_y, \omega_z\} = 2\pi \times \{28, 88, 66\}$ Hz. We then quench the magnetic field to the desired value and hold the cloud for 20 ms before performing a 30-ms-long time-of-flight. A magnetic field gradient ensures that the cloud does not fall due to gravity.

The scattering length is derived from a mean-field approach that incorporates dipolar interactions [32]. We write

$$a \approx a_{\text{stab.}} + \left(\frac{3R_x R_y}{2}\right)^{5/2} \times \frac{1}{CN},$$
 (14)

where $a_{\rm stab.} \approx 100\,a_0$ is the scattering length below which the BEC is no longer a stable solution in our trap geometry, a_0 is the Bohr radius, and $\mathcal{C} \propto a_{\rm ho}^4$.

We study the variation of the cloud size for different magnetic fields and show in Fig. 6 the resonances for which a clear dilatation is observed. We interpret this variation as a change in the scattering length using Eq. (14). Of the 11 loss features studied in this article, only 6 show a clear change in the size of

 $^{^4}$ We calibrate the magnetic field by transferring a small population in different Zeeman sublevels with a radio-frequency antenna. Due to dipolar relaxation, this process leads to losses when the frequency is resonant with the Zeeman splitting energy $\propto B$. We observed a small drift $\approx 1 \, \text{mG}$ between different days, which may be due to the stability of our magnetic field or the resolution of the calibration technique.

⁵Within the Thomas-Fermi approximation, $\mathcal{C}=15a_{\mathrm{ho}}^4(\frac{\tilde{\omega}^2}{\omega_x\omega_y})^{5/2}$, where $a_{\mathrm{ho}}=\sqrt{\frac{\hbar}{m\tilde{\omega}}}$ is the harmonic oscillator length. For our trap frequencies we get $\mathcal{C}\approx 31.54\,\mathrm{\mu m}^4$.

the BEC. These resonances are also the ones with the highest loss rate. Since the measurements are performed with a BEC, we cannot extract negative scattering lengths and report only positive values of a. We compare our measurements with those reported in Ref. [33] and find a good agreement for the scattering length evolution near the $B = 5.130 \,\text{G}$ Fano-Feshbach resonance.

Regarding the only three-body dominated loss feature at B = 5.561 G [see Fig. 6(f)], we draw the reader's attention to the interpretation of a BEC size change due to a variation of a. Since we do not exclude the existence of a pure three-body microscopic process for this resonance, a change in BEC size could also be due to pure three-body interactions and thus not to a change in scattering length. For harmonic traps this implies a change in the total area $\propto N^{1/2}$ (instead of $N^{2/5}$ for two-body interactions). We have tested this hypothesis by varying the number of atoms in the BEC. Although our results are consistent with $N^{2/5}$ scaling, we cannot exclude the $N^{1/2}$ result within our experimental uncertainties. It would be particularly interesting to study this resonance in a flat-bottom trap, where the size of the BEC area after time-of-flight will be proportional to N^3 for three-body interactions instead of N^2 for two-body interactions, leading to an easier lift of ambiguity. However, this study is beyond the scope of this article.

VI. CONCLUSION

We have characterized 11 low-field resonant loss features of an ultracold thermal sample of dysprosium. From the analysis of their density and temperature dependence, we conclude that most loss features result from a resonant *s*-wave pairwise interaction. We also measured the corresponding change in scattering length through the expansion of a BEC. Additionally, we measured the three-body loss rate of a quasi-pure BEC near zero magnetic field, which provides valuable information for future studies aimed at exploiting spin-orbit coupling in a dense condensate of dysprosium atoms [20].

Furthermore, we have evidenced (i) a possible two-body d-wave resonance, unobserved so far, highlighting the complex nature of interactions in strongly dipolar gases, and (ii) a loss resonance that may be controlled by pure three-body interactions. To go further in our quantitative description of three-body resonances, whether driven by two-body or three-body processes, we will need to better disentangle the roles of temperature and density, which should be possible with the preparation of a homogeneous sample of dysprosium in a boxlike trap [34].

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APPENDIX A: TWO-VERSUS THREE-BODY LOSS RATES TRIGGERED BY THREE-BODY RECOMBINATION PROCESSES

We consider the three-body recombination process at the core of our loss features. In particular, we consider the following consecutive pairwise reactions:

$$(1)A + A \underset{\Gamma'}{\overset{\Gamma}{\rightleftharpoons}} A_2^*$$

$$(2)A_2^* + A \xrightarrow{\Gamma_d} A_2 + A'.$$

Dismissing the coherence of process (1), we can express the "free" atomic and dimer dynamics by the coupled equations

$$\dot{n_a} = -2\Gamma n_a^2 + 2\Gamma' n_d^* - \Gamma_d n_a n_d^*
\dot{n_d^*} = \Gamma n_a^2 - \Gamma' n_d^* - \Gamma_d n_a n_d^*,$$
(A1)

where Γ is the volume rate to form an excited dimer from two free atoms, Γ' is the reverse process rate, and Γ_d is the volume loss rate to deeply bound dimers. The atomic density in the box is given by $n = n_a + 2n_d^*$, and for $\Gamma_d = 0$ there are no losses. We emphasize that we consider three-body recombination processes as the only loss mechanism.

These equations can be further simplified by introducing the volume $V_0 = \Gamma/\Gamma'$ and the renormalization time $t_0 = 1/\Gamma'$. We introduce the dimensionless quantities $A = V_0 n_a$ and $D = V_0 n_d^*$ such that the rate equations can be expressed in a dimensionless form,

$$\dot{A} = -2A^2 + 2D - bAD,\tag{A2}$$

$$\dot{D} = A^2 - D - bAD,\tag{A3}$$

where $b = \Gamma_d/\Gamma$.

Assuming that the population of excited dimers is zero at t = 0, we find numerically two different behaviors:

(1) For $b \gg 1$, the population in the excited dimers converges to $D(t) \approx A(t)/b$, as long as $bA \gg 2$. Since $b \gg 1$ we conclude that $D(t) \ll A(t)$ and thus the total atomic density, N = A + 2D, evolves as

$$\dot{N} \approx \dot{A} \approx -3A^2 \approx -3N^2$$
. (A4)

Although three-body losses are still the underlying process causing losses, the feature has a characteristic two-body loss behavior, i.e., $\dot{N} \propto -N^2$, leading to $1/N(t) \propto L_2 t$, as shown in Fig. 7(a).

(2) For $b \ll 1$, and $A \ll 1$, the population in excited dimers quickly *locks* to the atomic density squared, such that $D(t) \approx A(t)^2$. Since $D(t) \ll A(t)$ for all times, we then recover the time evolution for the total atomic density,

$$\dot{N} = \dot{A} + 2\dot{D} \approx -3bA^3 \approx -3bN^3,\tag{A5}$$

which has a characteristic three-body loss behavior, i.e., $\dot{N} \propto -N^3$, leading to $1/N^2(t) \propto L_3 t$ [see Fig. 7(b)].

APPENDIX B: DETAILS OF THE EXPERIMENTAL SETUP

1. Production of a ¹⁶²Dy MOT

We load 3×10^8 atoms in a magneto-optical trap (MOT), with a loading rate of 1×10^8 atoms/s, composed of five

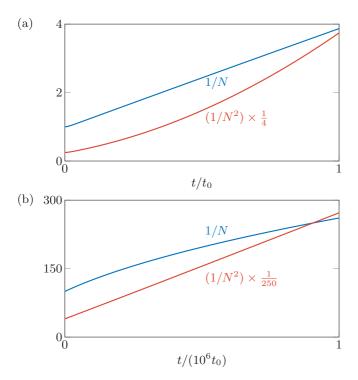


FIG. 7. (a) 1/N(t) (blue) and $1/N^2(t)$ (red) as a function of time t/t_0 for A(0) = 1 and b = 100. (b) 1/N(t) (blue) and $1/N^2(t)$ (red) as a function of time t/t_0 for A(0) = 0.01 and b = 0.01.

red-detuned beams (four in the x-y plane and one vertical), with detuning $\Delta_{MOT} = -43 \times \Gamma_{red}$, with respect to the intercombination line with vacuum wavelength $\lambda = 626.08 \, \text{nm}$ (red transition) and linewidth $\Gamma_{\rm red} \approx 2\pi \times 136\,{\rm kHz}$ [35]. The MOT is produced with a saturation parameter $s_0 = I_0/I_{\rm sat.} \approx$ 185 (the vertical beam has a tenth of this intensity) and a magnetic field gradient $\partial_z B_z = 1.72 \,\mathrm{G/cm}$. The cloud lies a few millimeters below the zero field, which makes it fully polarized in the Zeeman sublevel of lowest energy $|J, m_J|$ -J). The MOT capture velocity, determined by the linewidth of the transition and the MOT beam waist, $w_{\text{MOT}} = 15 \,\text{mm}$, is equal to $v_c \approx 7 \,\mathrm{m/s}$. We maximize the atomic flux reaching the main science chamber using an optical collimation. It is achieved through the cooling provided by a transverse molasses consisting of two retroreflected laser beams with orthogonal propagation with respect to the oven's exit axis. The molasses laser beams are red detuned, with detuning $\Delta_{\text{Coll.}} = -0.4 \times \Gamma_{\text{blue}}$, with respect to the optical transition with vacuum wavelength of 421.29 nm (blue transition) and linewidth $\Gamma_{\text{blue}} \approx 2\pi \times 32 \, \text{MHz}$. A saturation parameter of $s_0 = 4$ is used, leading to a fivefold increase in the loading rate of the MOT. The longitudinal velocity of the atomic flux exiting the oven is reduced from $v_x \approx 400 \,\mathrm{m/s}$ to $\approx 7 \,\mathrm{m/s}$ in a 500-mm Zeeman slower in a spin-flip configuration, with a laser beam detuning of $\Delta_{\text{Zeeman}} = -14 \times \Gamma_{\text{blue}}$ and a saturation parameter of $s_0 \approx 1$. The blue and red laser beams are frequency stabilized through modulation frequency transfer using either the atomic flux at the output of the oven (for the blue transition) or an iodine cell (for the red transition) [36].

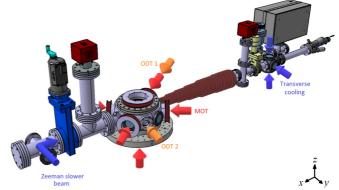


FIG. 8. Schematic representation of the experimental setup. The atoms are optically collimated at the output of the oven (transverse cooling) and then decelerated in a spin-flip Zeeman slower. The atoms are then confined in a magneto-optical trap (MOT) that comprises five laser beams and a magnetic field gradient. We compress the MOT and capture approximately 4×10^6 atoms into a crossed dipole trap (CDT) made up of two beams (ODT1 and ODT2) with a relative angle of 144° .

2. Compressed MOT and transfer into a crossed dipole trap

To further cool the atomic cloud, we reduce the saturation parameter of the red lasers to $s_0 = 5.7$, decrease the detuning to $\Delta_{\rm cMOT} = -21 \times \Gamma_{\rm red}$, and increase the gradient to $\partial_z B_z = 4.31$ G/cm, which stabilizes the position of the cloud against small fluctuations in the laser frequency and magnetic field. Although it leads to a compressed MOT (cMOT) with a temperature $T \approx 15 \, \mu \rm K$, higher than the Doppler temperature, it ensures a stable overlap with the crossed dipole trap (CDT). The cMOT has a typical size at $1/\sqrt{e}$ of 400 μm and atom number $\sim 1 \times 10^8$.

The CDT is composed of two single-mode laser beams at a wavelength of 1064 nm, with a relative angle of 144° in the x-y plane, and a frequency difference of 180 MHz, which ensures that residual interference patterns are averaged out. As we reduce the detuning of the MOT beams, light-induced loss processes are enhanced, resulting in a short lifetime of the cMOT (\sim 200 ms). The loading of the cMOT into the CDT is therefore fast, $\sim 50 \,\mathrm{ms}$, which allows us to load 4×10^6 atoms at a temperature of 60 µK. The two beams that make up the CDT, hereafter identified as ODT1 and ODT2 (see Fig. 8), have waists $w_{\rm ODT1} \approx 30 \, \mu \rm m$ and $w_{\rm ODT2} \approx 20 \, \mu \rm m$. To optimize the loading, we enlarge the waist of ODT1 in the x-yplane by a factor of 2 with an acousto-optic deflector [37]. The two optical dipole trap beams have maximum powers of 30 W (ODT1) and 5 W (ODT2), and the forced evaporative cooling is performed in the presence of a bias field aligned along the z direction and with magnitude $B_z = 1.660 \,\mathrm{G}$. The maximum loading efficiency is achieved for horizontally polarized dipole beams. This is because the difference in polarizability between the ground and excited states of the intercombination line, $\Delta \alpha = \alpha_{\rm exc.} - \alpha_{\rm ground}$, is negative at 1064 nm for a linear horizontal polarization [38]. This guarantees that the detuning of the cMOT cooling beam remains negative. After loading the CDT and prior to evaporative cooling, we rotate the polarization of ODT2 by 90°.

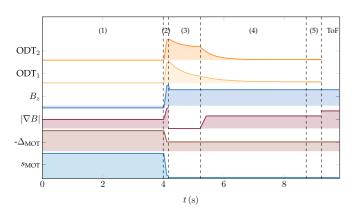


FIG. 9. Schematic representation of the experimental sequence used to produce a degenerate gas of dysprosium. (1) MOT loading stage. (2) Compressed MOT. (3) First stage of evaporative cooling. (4) Second stage of evaporative cooling. (5) Plain evaporation in the CDT to purify the quantum gas. (ToF) Time-of-flight expansion and absorption imaging acquisition.

3. Crossed dipole trap evaporative cooling

The first evaporation stage lasts for 1 s, during which we suppress the spatial modulation of ODT1 and reduce its power so that the two beams forming the crossed dipole trap have similar trap depths. We focus here on the second stage of forced evaporative cooling, which lasts for 3.5 s (see Fig. 9). At the beginning of this evaporation, we switch on a magnetic field gradient to partially compensate for gravity, which plays an important role in the optimization of the evaporative cooling [39].

We measure both temperature, atom number, and trap frequencies at different times during the second evaporative cooling stage. In Figs. 10(a) and 10(b) we show the evolution of temperature and atom number as a function of time. Combined with our measurements of the trap frequencies, we compute the evolution of the averaged phase-space density $\mathcal{D} = n_a \lambda^3$, where n_a takes into account the averaging over the inhomogeneous density in the harmonic potential (see main text). We show in Fig. 10(c) the evolution of \mathcal{D} as a function of N_a in log-log scale. From the fit function $\mathcal{D} \propto N_a^{-\vartheta}$, we determine the evaporative cooling efficiency $\vartheta \approx 4$ at the upper end of typical values in optical dipole traps $(2 \lesssim \vartheta \lesssim 5)$ [39].

4. Examples of expanded clouds in the vicinity of the 5.130-G Feshbach resonance

We here present some examples for the BEC expansion near the $B_0 = 5.130 \, \mathrm{G}$ Feshbach resonance discussed in Fig. 6(e). We deduce the change in scattering length from the cloud dilatation in the x-y plane after a 30-ms time-of-flight. As shown in Fig. 11(a), the expansion of the BEC far from the resonance, for instance, $B = 4.886 \, \mathrm{G}$ (yellow dot), leads to radii of 30–45 $\mu \mathrm{m}$, along the two orthogonal axes of the optical dipole trap in the x-y plane. As the scattering length increases, the cloud expands significantly more, as shown in Fig. 11(b) for a magnetic field of $B = 5.109 \, \mathrm{G}$. Interestingly, for $B > B_0$, where the scattering length passes from large negative values

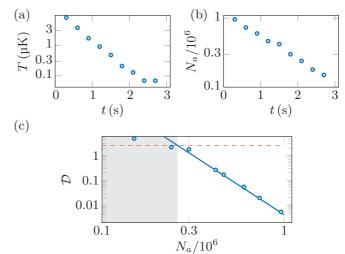


FIG. 10. Efficiency of evaporative cooling. (a) Temperature as a function of time in log-linear scale. (b) Atom number as a function of time in log-linear scale. (c) Phase-space density (\mathcal{D}) as a function of atom number, N_a , in log-log scale. We fit our data with $\mathcal{D} \propto N_a^{-\vartheta}$ and retrieve $\vartheta \approx 4.0$. The gray region indicates the points for which a non-negligible condensed fraction is already present and the estimation of \mathcal{D} is no longer quantitative. The horizontal dashed line corresponds to the noninteracting prediction for the emergence of a BEC at $\mathcal{D} \approx 2.612$.

to its background value and thus crosses zero, we observe a cloud that does not expand even after a long time-of-flight [see Fig. 11(c)], which is a hallmark of quantum droplets [40]. Our procedure for determining the scattering length cannot be used in this case, as one would need to incorporate beyond-mean-field corrections to explain the stability of the cloud.

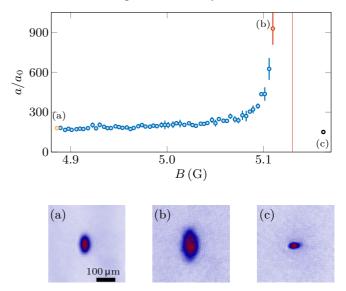


FIG. 11. Scattering length in the vicinity of the $B_0 = 5.130 \,\mathrm{G}$ resonance (vertical red line). Expansion of a BEC in the x-y plane after 30-ms time-of-flight, (a) far from the Feshbach resonance and near the resonance with $B < B_0$ (b) or $B > B_0$ (c). We interpret the strong expansion of the BEC for $B < B_0$ resulting from a large scattering length, while for $B > B_0$ we observe a dense cloud compatible with the formation of quantum droplets.

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